## Week 9-Lab 1: Worksheet 12: Sections 15.2 and 15.3

They said: "What is the point of quizzes again?" I said:" To get you to study in small chunks in a low stake setting. (Each are $0.5 \%$ of your grade?!) " I added: "Have you seen a kid with Halloween candy? They want to eat all they collected at once; they are not worried about tomorrow with no candy. Human tend to indulge. For most of us, there has to be an obvious incentive to get the work done." I also said:" Have you been doing the Diagnostic quizzes?"

## Triple integrals:

Use geometry of the picture to find two surfaces that bound the inner variable. This step does not require eliminating a variable between two equations.

After the inner integral is set. Find the reflection of the solid on the coordinate plane of the two variable. Treat the two outer integrals as a double integral on the region of reflection. This step may require eliminating a variable between two equations.

## Non-simple Regions:

Divide into simple regions and set one iterated integral for each.

## Group Work Portion of Worksheet

Names:
Work in groups to do this portion of the worksheet. Make sure to take parts in solving the problems. Your participation score is a combination of being prepared, willing to explore the problem, working in groups and contributing toward the solution.

1. Background Story: Please review double integral from before the break (Monday and Wednesday lab sections only.) The integrand can represent height, mass density, charge density and many more. In the next question, it is the mass density.
Question(s): Sketch the region of integration and find the mass of the lamina that occupies the region $\mathcal{D}$ and density $\rho(x, y)=y$ where $\mathcal{D}$ is bounded by $y=e^{x}, y=0, x=0$, and $x=2$.
2. (A) Consider $\int_{0}^{2} \int_{0}^{x^{2} / 4} \int_{0}^{5 y} f(x, y, z) d z d y d x$. Explain to each other why the following figure is the solid of the integration. (You do not have to write this part down.)

(B) Which of the following is an iterated integrals that is equal to $\int_{0}^{2} \int_{0}^{x^{2} / 4} \int_{0}^{5 y} f(x, y, z) d z d y d x$. Explain why the other three answers are NOT correct.
(A) $\int_{0}^{1} \int_{2 \sqrt{y}}^{2} \int_{0}^{5 x^{2} / 4} f(x, y, z) d z d x d y$
(C) $\int_{0}^{1} \int_{2 \sqrt{y}}^{2} \int_{0}^{5 y} f(x, y, z) d z d x d y$
(B) $\int_{0}^{1} \int_{0}^{2 \sqrt{y}} \int_{0}^{5 x^{2} / 4} f(x, y, z) d z d x d y$
(D) $\int_{0}^{1} \int_{0}^{2 \sqrt{y}} \int_{0}^{5 y} f(x, y, z) d z d x d y$
(C) On the above figure, mark the two surfaces bounding the most inner integral in the order $d y d z d x$.
(D) Write four iterated integrals that are equal to $\int_{0}^{2} \int_{0}^{x^{2} / 4} \int_{0}^{5 y} f(x, y, z) d z d y d x$ in these orders:
(i) $d x d z d y$ :

The inner integral bounds are:

$$
\square \leq x \leq \square
$$

The region for the two outer integrals:


(iii) $d y d z d x$ :

The inner integral bounds are:

$$
\square \leq y \leq \square
$$

The region for the two outer integrals:

(ii) $d x d y d z$ :

The inner integral bounds are:

$$
\square \leq x \leq \square
$$

The region for the two outer integrals:

(iv) $d y d x d z$ :

The inner integral bounds are:

$$
\square \leq y \leq \square
$$

The region for the two outer integrals:



Video: https://youtu.be/4HAw9ttQvoE
Gegebra Sheet: https://www.geogebra.org/m/mnw4gbyz
3. Background Story: The following solid is not simple in y-direction.

Question(s): Use triple integrals to find the volume of the solid in the first octant which is bounded by the coordinate planes, $y+z=4$, and $x=16-y^{2}$.

(A) The solid integral is non-simple $y$-direction. The graph shows the two regions, $\mathcal{A}$ and $\mathcal{B}$, where the outer integrals can be set up as two $y$-simple solids. Find curve $g$. Find the values $a$ and $b$. Find the bounds in $y$-direction.

(B) Set up the integral in the non-simple $y$-direction using Part (A). (Either use $d y d x d z$ order or $d y d z d x$ order.)
(C) Set up the integral in $d z d x d y$ order or $d z d y d x$ order.
(D) Evaluate the volume.
4. Background Story: Sometimes the solid is described and we need to find the shape of it. (Tuesday and Thursday lab Sections can skip due to lack of time.)
Question(s): Find the volume of the solid bounded below $z=3$ and above the plane containing the points $(0,0,4),(0,4,0)$, and $(4,0,0)$ in the first octant.

GroupWork Rubrics:
Preparedness: _-/0.5, Contribution: __/0.5, Correct Answers: _-/0.5

## Individual Portion of Worksheet

## Name:

$\qquad$
Upload this section individually on canvas or turn it in to your instructor on the $2^{\text {nd }}$ lab day of the week. You can ask questions in class and work in groups but you turn in the individual work. Start before the class so you can ask questions during the class. If you didn't complete the work in class, make sure to work on it outside the class and complete it. Show all your work; your score depends on the work you have shown.

GroupWork Rubrics day 2:
Preparedness: __/0.5, Contribution: __/0.5, Correct Answers: __/ 0.5
5. (3.5 points) Find the volume of the solid enclosed by $z=4, y=0, y=25-x^{2}$, and $z+y=29$.

6. Set up, do not solve, three equivalent iterated triple integrals representing

$$
\int_{0}^{4} \int_{0}^{16-y^{2}} \int_{0}^{2 y} f(x, y, z) d z d x d y
$$

in orders
(A) (1 point) $\int \begin{aligned} & \square \\ & \square \\ & \square \\ & \square \\ & \square \\ & \square\end{aligned}(x, y, z) f(x, y, z) d z d y d$ 南 $_{\square}^{\square} z=2 y$

(B) (1 point) $\int \square \int \square \int \square \square \square$
$(16,0,0) x^{7}$
(C) (1.5 points) $\int_{\square}^{\square} \int \square \int \square f(x, y, z) d y d z d x$

